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Payload and Resistance Optimization of a SWATH Model via Design Space Dimensionality Reduction, CFD, and Multi-fidelity Surrogate Models

R. Pellegrini¹, A. Serani¹, S. Harries², and M. Diez¹

¹CNR-INSEAN, National Research Council - Marine Technology Research Institute, Rome, Italy {riccardo.pellegrini,andrea.serani}@insean.cnr.it; <u>matteo.diez@cnr.it</u> ²Friendship Systems AG, Potsdam, Germany harries@friendship-systems.com

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Outline

- Introduction
 - CNR-INSEAN
 - Background of simulation-based design optimization (SBDO)
 - Objective: multi-objective optimization problem
 - > Approach
- Design-space dimensionality reduction by Karhunen-Loève Expansion
- SWATH geometry variations from CAESES
- CFD code WARP
- Adaptive multi-fidelity metamodel
- Multi-objective deterministic particle swarm optimization algorithm

- Numerical results
- Conclusions and future work







CNR-INSEAN: Marine Technology Research Institute, Italy

CNR-INSEAN: Numerical / Experimental research on naval hydrodynamics and marine engineering;
145 people (65 researchers, research engineers and temporary positions); *All in-house: simulation codes & hardware (design, production, testing).*

- Numerical modeling and simulations for hydrodynamics of hull, propeller, wave breaking, sloshing, hydroacoustics, structures
- Simulation-based design methods including validation experiments









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- Towing tanks
- Circulating water channel
- Cavitation tunnel
- Maneuvering basin (Nemi Lake)

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- Hydraulic channel
- Sloshing lab
- High-speed ditching
- Mechanical, electronic, equipment workshops
- Woodshop

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Simulation-based design optimization



Multi-objective optimization problem

- The optimization addresses
 - \succ total resistance (R_T) minimization (18 kn)
 - payload maximization (∇) \succ

	Value [m]	Dimension	
	36.50	L _{OA}	
	4.50	D	
	20.00	D _H	
	6.00	L ₁	
No const	12.00	SL	
are impos	5.15	S _C	
this preli	6.31	т	
арриса	1064 [m²]	Sw	
	38.88 [m ²]	A _{WP}	
_			
			-

Objective functions	Value		
∇	982.23 [m ³]		
R _T (HF, 18 kn)	4.816E5 [N]		

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Pellegrini R., Serani A., Harries S., and Diez M. "Multi-objective hull-form optimization of a SWATH configuration via design-space dimensionality reduction, multi-fidelity metamodels, and swarm intelligence" In proceedings of 7th International conference on Computational Methods in Marine Engineering (MARINE 2017), 15-17 May 2017, Nantes, France. Narine Technology Research Institute

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Approach - INSEAN SBDO Framework



Design-space dimensionality reduction - Underlying idea



- Before going through the optimization process, one does not know (yet) where the optimal design is
- The optimum is unknown and its identification may be considered as a problem affected by *epistemic uncertainty* (Diez et al., CMAME, 2015)
- One may consider the (uncertain) design variable vector u as belonging to a stochastic domain $\mathcal U$ with associated probability density function $f(u), u \in \mathcal U$

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Diez, M., Campana, E. F., & Stern, F. (2015). Design-space dimensionality reduction in shape optimization by Karhunen–Loève expansion. *Computer Methods in Applied Mechanics and Engineering*, 283, 1525-1544.

Design-space dimensionality reduction - Definitions



 $m{u}$ design variable (uncertain) $m{x}$ spatial variable $\langle \cdot \rangle$ ensamble average over $m{u}$ $m{\delta} = m{\delta} - \langle m{\delta} \rangle$ $ho(m{x})$ weight function Generalized inner product

$$(\boldsymbol{f}, \boldsymbol{g})_{\rho} = \int_{\mathcal{G}} \rho(\boldsymbol{x}) \boldsymbol{f}(\boldsymbol{x}) \cdot \boldsymbol{g}(\boldsymbol{x}) d\boldsymbol{x}$$

Mean shape modification

$$\langle \boldsymbol{\delta} \rangle = \int_{\mathcal{U}} \boldsymbol{\delta}(\boldsymbol{x}, \boldsymbol{u}) f(\boldsymbol{u}) d\boldsymbol{u}$$

Geometric variance (key element)

$$\sigma^{2} = \langle ||\widehat{\delta}||^{2} \rangle$$
$$= \int_{\mathcal{U}} \int_{\mathcal{G}} \rho(\mathbf{x}) \widehat{\delta}(\mathbf{x}, \mathbf{u}) \cdot \widehat{\delta}(\mathbf{x}, \mathbf{u}) f(\mathbf{u}) d\mathbf{x} d\mathbf{u}$$

Design-space dimensionality reduction – Problem statement

Basis of orthonormal functions (KLE)

$$\widehat{\delta}(\boldsymbol{x}, \boldsymbol{u}) = \sum_{k=1}^{\infty} \alpha_k(\boldsymbol{u}) \boldsymbol{\varphi}_k(\boldsymbol{x})$$

 $m{u}$ design variable (uncertain) $m{x}$ spatial variable $\langle \cdot \rangle$ ensamble average over $m{u}$ $m{\delta} = m{\delta} - \langle m{\delta} \rangle$ $ho(m{x})$ weight function

- Geometric variance expressed as $\sigma^{2} = \sum_{k=1}^{\infty} \sum_{j=1}^{\infty} \langle \alpha_{k} \alpha_{j} \rangle (\boldsymbol{\varphi}_{k}, \boldsymbol{\varphi}_{j})_{\rho} = \sum_{j=1}^{\infty} \langle \alpha_{j}^{2} \rangle = \sum_{j=1}^{\infty} \langle (\widehat{\boldsymbol{\delta}}, \boldsymbol{\varphi}_{j})_{\rho}^{2} \rangle$
- Formulation of a variational problem

$$\max_{\boldsymbol{\varphi} \in \mathcal{L}^{2}_{\rho}(\mathcal{G})} \boldsymbol{J}(\boldsymbol{\varphi}) = \left\langle \left(\widehat{\boldsymbol{\delta}}, \boldsymbol{\varphi}_{j} \right)_{\rho}^{2} \right\rangle$$

subject to $(\boldsymbol{\varphi}, \boldsymbol{\varphi})_{\rho}^{2} = \mathbf{1}$

The variational problem solution is

$$\mathcal{L}\boldsymbol{\varphi}(\boldsymbol{x}) = \int_{\mathcal{G}} \langle \delta(\boldsymbol{x}, \boldsymbol{u}) \otimes \delta(\boldsymbol{y}, \boldsymbol{u}) \rangle \boldsymbol{\varphi}(\boldsymbol{y}) d\boldsymbol{y} = \lambda \boldsymbol{\varphi}(\boldsymbol{x})$$

Design-space dimensionality reduction – Discretization

Considering the variational problem solution

$$\mathcal{L}\boldsymbol{\varphi}(\boldsymbol{x}) = \int_{\mathcal{G}} \langle \delta(\boldsymbol{x}, \boldsymbol{u}) \otimes \delta(\boldsymbol{y}, \boldsymbol{u}) \rangle \boldsymbol{\varphi}(\boldsymbol{y}) d\boldsymbol{y} = \lambda \boldsymbol{\varphi}(\boldsymbol{x})$$

• Define a 3-D (cartesian) basis of orthogonal unit vector $\{e_q\}_{q=1}^3$ is possible to write

$$\boldsymbol{\delta}(\boldsymbol{x},\boldsymbol{u}) = \sum_{q=1}^{3} \delta_q(\boldsymbol{x},\boldsymbol{u})\boldsymbol{e}_q, \qquad \boldsymbol{\varphi}(\boldsymbol{x}) = \sum_{q=1}^{3} \varphi_q(\boldsymbol{x})\boldsymbol{e}_q$$

which yields

$$\sum_{q=1}^{3} \int_{\mathcal{G}} \left\langle \delta_{p}(\boldsymbol{x}, \boldsymbol{u}) \delta_{q}(\boldsymbol{y}, \boldsymbol{u}) \right\rangle \varphi_{q}(\boldsymbol{y}) d\boldsymbol{y} = \lambda \varphi_{p}(\boldsymbol{x})$$

Discretizing the variable of integration y (therefore the geometry) with L elements of dimension ΔG_j and centroid at $x_j, j = 1, ..., L$

$$\sum_{q=1}^{\infty}\sum_{j=1}^{\infty} \langle \delta_p(\boldsymbol{x}_i, \boldsymbol{u}) \delta_q(\boldsymbol{x}_j, \boldsymbol{u}) \rangle \varphi_q(\boldsymbol{x}_j) \Delta \mathcal{G}_j = \lambda \varphi_p(\boldsymbol{x}_i)$$

Design-space dimensionality reduction – Implementation



Design-space dimensionality reduction – Implementation



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Design-space dimensionality reduction – Implementation

This form can be discretized as

$$\sum_{q=1}^{3} \sum_{j=1}^{L} \langle \delta_{p}(\boldsymbol{x}_{i}, \boldsymbol{u}) \delta_{q}(\boldsymbol{x}_{j}, \boldsymbol{u}) \rangle \varphi_{q}(\boldsymbol{x}_{j}) \Delta \mathcal{G}_{j} = \lambda \varphi_{p}(\boldsymbol{x}_{i})$$

$$\mathbf{d}_{p}(\mathbf{u}) = \begin{cases} \gamma_{p}(\boldsymbol{x}_{1}, \boldsymbol{u}_{k}) \\ \vdots \\ \gamma_{p}(\boldsymbol{x}_{L}, \boldsymbol{u}_{k}) \end{cases} - \frac{1}{S} \sum_{k=1}^{S} \begin{cases} \gamma_{p}(\boldsymbol{x}_{1}, \boldsymbol{u}_{k}) \\ \vdots \\ \gamma_{p}(\boldsymbol{x}_{L}, \boldsymbol{u}_{k}) \end{cases} \mathbf{z}_{p}$$

$$\gamma_{p} = \boldsymbol{\gamma} \cdot \boldsymbol{e}_{p}$$

$$\boldsymbol{D}_{p} = [\mathbf{d}_{p}(\mathbf{u}_{1}) \quad \dots \quad \mathbf{d}_{p}(\mathbf{u}_{S})]$$

$$\boldsymbol{R}_{pq} = \frac{1}{S} \boldsymbol{D}_{p} \boldsymbol{D}_{q}^{T} \quad \text{Covariance matrix}$$

$$\boldsymbol{W} = [\Delta \mathcal{G}_{i} \delta_{ij}]$$

$$\mathbf{Az} = \lambda z$$

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LAESE

Design-space dimensionality reduction – "How to use"

 Property: each eigenvalue (KL value) equal the variance retained by the associated eigenfunction (KL mode)

variance retained by each KLE eigenfunction

 $\lambda_k = \langle \alpha_k^2 \rangle$



Dimensionality reduction with confidence level I

$$\widehat{\boldsymbol{\delta}}(\boldsymbol{x},\boldsymbol{\lambda}) = \sum_{k=1}^{N} \alpha_{k}(\boldsymbol{x}) \varphi_{k}(\boldsymbol{x})$$
New design variables
New representation of the shape modification (new design space, ROM)

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$$\sum_{k=1}^{N} \lambda_k \ge l \sum_{k=1}^{\infty} \lambda_k = l\sigma^2$$

N is the new (reduced) dimensionality of the design space

Design-space dimensionality reduction – "How to use"

Property: each eigenvalue (KL value) equal the variance retained by the associated eigenfunction (KL mode)

variance retained by each KLE eigenfunction

 $\lambda_k = \langle \alpha_k^2 \rangle$



Dimensionality reduction with confidence level I



Design-space dimensionality reduction – "How to use"

 Property: each eigenvalue (KL value) equal the variance retained by the associated eigenfunction (KL mode)

variance retained by each KLE eigenfunction

 $\lambda_k = \langle \alpha_k^2 \rangle$



Dimensionality reduction with confidence level I



Before optimization – Reference geometry modifications

Reference geometry variations









Results

- The eigenvalues are convergent with respect to the number of designs,
- 4 modes are sufficient for retaining more than 95% of the original variance,
- From 27 to 4 variables, more than 85% dimensionality reduction.



• First four KL modes φ









• First four KL modes φ



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• First four KL modes φ



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• First four KL modes φ



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• First four KL modes φ



Potential flow solver

- Wave Resistance Program (WARP)
 - Fixed body
 - Double model linearization
 - Intel Xeon E5-1620 v2 @3.70GHz
 - > HF steady linear potential flow code
 - fine body/surface grids
 - 4 minutes wall-clock time
 - > LF steady linear potential flow code
 - coarse body/surface grids
 - 1 minute wall-clock time

Grid	G1	G2	
Upstream extension	1.5	L _{OA}	
Downstream extension	3.5	L _{OA}	
Sideways extension	1.5 L _{OA}		
Body panels	5.2 k	2.6 k	
Surface panels	6.0 k	3.0 k	



Bassanini et al., The Wave Resistance Problem in a Boundary Integral Formulation, Surveys on Mathematics for Industry, 4:151-194, 1994.

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Potential flow solver

Sensitivity analysis



Adaptive multi-fidelity metamodel (AMFM)

AMFM

The adaptive sampling procedure is based on metamodel uncertainty minimization.



f_H –

H 🛇

LO

δ ---

Pellegrini R., Iemma U., Leotardi C., Campana E.F., Diez M., "Multi-fidelity adaptive global metamodel of expensive computer simulations", in Proceedings of IEEE World congress on computational intelligence (WCCI) 24-29 July 2016, Vancouver, Canada.

Adaptive multi-fidelity metamodel (AMFM) - Results

- AMFM uncertainty convergence
 - > The sensitivity analysis is also the training set (17 HF and LF simulations)
 - > Available budget of 100 iterations



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Multi-objective deterministic particle swarm optimization

MODPSO

- > Meta-heuristic algorithm based on the metaphor of a flock of bird or bees searching for food [2]
- > **Personal attractor**: minimum of the aggregated function
- > Global attractor: closest point of social solution set
- > Hammersley sequence sampling initialization over domain and boundaries, with non-null velocity
- 8N_{dv}N_{of} particles
- χ=0.721
- ▷ $c_1 = c_2 = 1.655$



R. Pellegrini, A. Serani, C. Leotardi, U. Iemma, E.F. Campana, M. Diez, "Formulation and parameter selection in multi-objective deterministic particle swarm for simulation-based optimization", Applied Soft Computing 58 (2017) 714-731. pp. 1942–1948.

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Simulation-based hull-form optimization

- Non-dominated solution set and most promising configurations performances
 - The optimization is performed with a deterministic formulation of multi-objective particle swarm optimization algorithm



		$\Delta R_T \%$ $\Delta \nabla \%$		ΔR _T %		%	
Design	ΔL _{OA} %	ΔS _w %	ΔA _{WP} %	AMFM	WARP	AMFM	WARP
А	20.55	19.60	-5.65	-28.30	-24.30	22.70	22.80
В	22.19	24.33	1.27	-19.20	-19.20	28.10	28.20
С	21.64	20.10	-11.42	-26.70	-25.70	25.20	25.10

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Optimized hull-form



Optimized hull-form

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Optimized hull-form



Conclusions

- The hull-form optimization of a SWATH model, addressing the total resistance reduction (at 18 kn) and the displacement maximization, has been presented
 - The parametric CAD models has been produced with CAESES[©] software
 - The geometric variations have been produced with the CAESES
 [©] Sobol engine
 - > The design-space has been reduced with the KLE method
 - The stochastic radial basis functions based multi-fidelity metamodel has been used to predict the model performances
 - The optimization has been performed with a deterministic formulation of multi-objective particle swarm optimization algorithm
- The design variables has been reduced from 27 to 4 (85% of reduction), retaining more than 95% of the original variance
- The AMFM maximum uncertainty has been reduced to 9.1% and 5.6% of the original function range for the total resistance and displacement, respectively
- 27 high- and 117 low-fidelity evaluations have been performed
- The optimal design achieves a reduction of the total resistance about 25% and an increase of the displacement about 25%





Ongoing/Future work

- Non-linear KLE [1]
 - E.g. deep auto-encoder
- Inclusion of physical parameters in KLE
 - The variational analysis takes into account also the physical effects of the geometry modification
- Use of high-fidelity CFD codes [2]
 - Xnavis, developed at CNR-INSEAN
- Use of hybrid global/local algorithms
 - Combination of MODPSO and linesearch-type algorithms
- Development of parallel strategies for the AMFM update

Take advantage of HPC cluster

[1]D'Agostino D., Serani A., Campana E.F., and Diez M. "Nonlinear Methods for Design-Space Dimensionality Reduction in Shape Optimization ", In proceedings of 3rd International conference on Machine learning, Optimization and Big Data (MOD 2017) 14-17 September, Volterra, Italy, 2017.
 [2]Pellegrini R., Serani A., Broglia R., Harries S., and Diez M., "Payload Optimization of a Sea Vehicle by Multi-Fidelity Surrogate Models", In preparation for 2018 AIAA SciTech Forum, 8–12 January 2018, Gaylord Palms, Kissimmee, Florida.







Thank you!

Questions ?? Suggestions ?!?!?!

